

# Interplay of Ring Puckering and Hydrogen Bonding in Deoxyribonucleosides

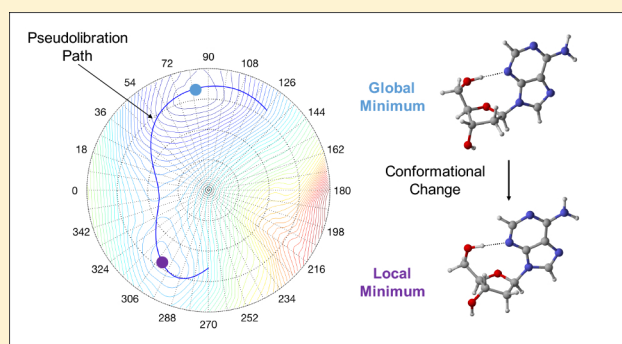
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## S Supporting Information

**ABSTRACT:** The Cremer–Pople ring puckering analysis and the Konkoli–Cremer local mode analysis supported by the topological analysis of the electron density were applied for the first comprehensive analysis of the interplay between deoxyribose ring puckering and intramolecular H-bonding in 2'-deoxycytidine, 2'-deoxyadenosine, 2'-deoxythymidine, and 2'-deoxyguanosine. We mapped for each deoxyribonucleoside the complete conformational energy surface and the corresponding pseudorotation path. We found only incomplete pseudorotation cycles, caused by ring inversion, which we coined as pseudolibration paths. On each pseudolibration path a global and a local minimum separated by a transition state were identified. The investigation of H-bond free deoxyribonucleoside analogs revealed that removal of the H-bond does not restore the full conformational flexibility of the sugar ring. Our work showed that ring puckering predominantly determines the conformational energy; the larger the puckering amplitude, the lower the conformational energy. In contrast no direct correlation between conformational energy and H-bond strength was found. The longest and weakest H-bonds are located in the local minimum region, whereas the shortest and strongest H-bonds are located outside the global and local minimum regions at the turning points of the pseudolibration paths, i.e., H-bonding determines the shape and length of the pseudolibration paths. In addition to the H-bond strength, we evaluated the covalent/electrostatic character of the H-bonds applying the Cremer–Kraka criterion of covalent bonding. H-bonding in the puric bases has a more covalent character whereas in the pyrimidic bases the H-bond character is more electrostatic. We investigated how the mutual orientation of the CH<sub>2</sub>OH group and the base influences H-bond formation via two geometrical parameters describing the rotation of the substituents perpendicular to the sugar ring and their tilting relative to the ring center. According to our results, rotation is more important for H-bond formation. In addition we assessed the influence of the H-bond acceptor, the lone pair (N, respectively O), via the delocalization energy. We found larger delocalization energies corresponding to stronger H-bonds for the puric bases. The global minimum conformation of 2'-deoxyguanosine has the strongest H-bond of all conformers investigated in this work with a bond strength of 0.436 which is even stronger than the H-bond in the water dimer (0.360). The application of our new analysis to DNA deoxyribonucleotides and to unnatural base pairs, which have recently drawn a lot of attention, is in progress.



## INTRODUCTION

Deoxyribonucleosides and their analogs are important building blocks for the synthesis of antiviral drugs and anticancer agents,<sup>1–3</sup> and the production of deoxyribonucleotides for polymerase chain reactions.<sup>4–6</sup> They can serve as biological probes.<sup>7</sup> Certain bacteria, e.g., the Gram-positive soil bacterium *Bacillus subtilis*, can utilize deoxyribonucleosides via the catabolic deoxyribonucleoside pathway as a source of carbon and energy.<sup>8</sup> The reverse deoxyriboaldolase enzyme (DERA)<sup>9</sup> can drive the deoxyribonucleoside synthesis showing great promise for industrial-scale production of deoxyribonucleosides.<sup>10,11</sup> The DERA pathway has recently attracted a lot of attention as a possible alternative to the production of

deoxyribonucleotides via ribonucleotide reductases (RNRs).<sup>9,12</sup> Therefore, understanding more about deoxyribonucleosides and their synthesis via the DERA pathway offers an important gateway to new mechanistic insights into this pathway, which could help us to understand the suggested DERA production of deoxyribonucleotides shedding more light onto the origin of DNA.<sup>12</sup> One important ingredient along this route is to understand the conformational flexibility of deoxyribonucleosides, which is determined by a complex

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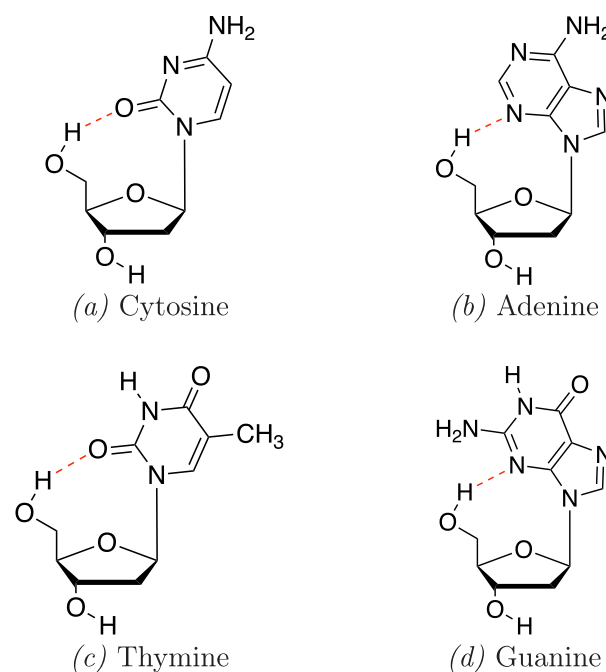


interplay of ring puckering of the deoxyribose sugar ring and intramolecular hydrogen bonding (H-bonding). So far, conformational studies of deoxyribonucleosides have focused mostly on either the ring puckering or the H-bonding aspect. In 1972, Altona and Sundaralingam<sup>13</sup> introduced a procedure describing both the puckering angle and puckering amplitude of a five-membered ring via torsional angles. However, the definition of the ring puckering amplitude expressed via an angle does not allow the appropriate description of the ring pseudorotation process. In this process, the maximum puckering amplitude is rotating around the edge of the ring without raising a substantial potential energy change. Such a movement can be best described with a puckering amplitude defined as displacement from a reference. Ring puckering and pseudorotation of nucleosides based on the Altona and Sundaralingam approach were able to describe the molecular properties of specific deoxyribose sugar ring conformations; however, they failed to describe the changes of molecular properties along the pseudorotation path in a smooth form.<sup>2,14–17</sup> Other studies focused on the influence of the intramolecular hydrogen bonds (H-bond)s on the conformational of deoxyribonucleosides.<sup>18–23</sup> They investigated predominantly the internal H-bonds between the base and the CH<sub>2</sub>OH group of the sugar ring. Other internal H-bonds resulting from a rotation of the base unit were not considered in a systematic fashion. Studies of the correlation between ring puckering and H-bonding have been rarely reported, even when the conformational energy surface (CES) was explored,<sup>24</sup> or when global reactivity parameters were derived.<sup>2</sup>

Therefore, the way that deoxyribose ring puckering affects the formation of internal H-bonding and vice versa is not fully understood yet. To understand the driving force of the conformational flexibility of deoxyribonucleosides it is important (i) to quantitatively assess both, ring puckering and H-bonding, and (ii) to investigate the relationship between these two essential structural features. We used in this work as an efficient tool a combination of the Cremer–Pople *ring puckering analysis*<sup>25–30</sup> and the *local mode analysis* of Konkoli and Cremer,<sup>31–34</sup> which describes the conformational process at the quantum mechanical level. In particular, the following objectives were included in our study:

- To exploit the CES, to determine the pseudorotation path and the location of the global and local minima on the CES for the deoxyribonucleosides **dC**, **dA**, **dT**, and **dG**; see Figure 1.
- To investigate how the conformational energy, the puckering amplitude, and the H-bond properties such as distance and bond strength change along the pseudorotation path of deoxyribose ring and how these changes are connected; as an important step to understand the interplay between sugar ring puckering and H-bonding.
- To monitor the change of the covalent character of the H-bonds along the pseudorotation path via the topological analysis of the electron density.

The paper is structured in the following way. In the second section the methods used in this work are described as well as computational details. The third section presents the results and discussion. Conclusions and an outlook are made in the final section.



**Figure 1.** Deoxyribonucleosides investigated in this work: (a) 2'-deoxycytidine (cytosine), **dC**, (b) 2'-deoxyadenosine (adenine), **dA**, (c) thymidine (thymine), **dT**, (d) 2'-deoxyguanosine (guanine), **dG**. The red dashed line indicates the internal H-bond between the base and the CH<sub>2</sub>OH substituent of the sugar ring.

## METHODOLOGIES

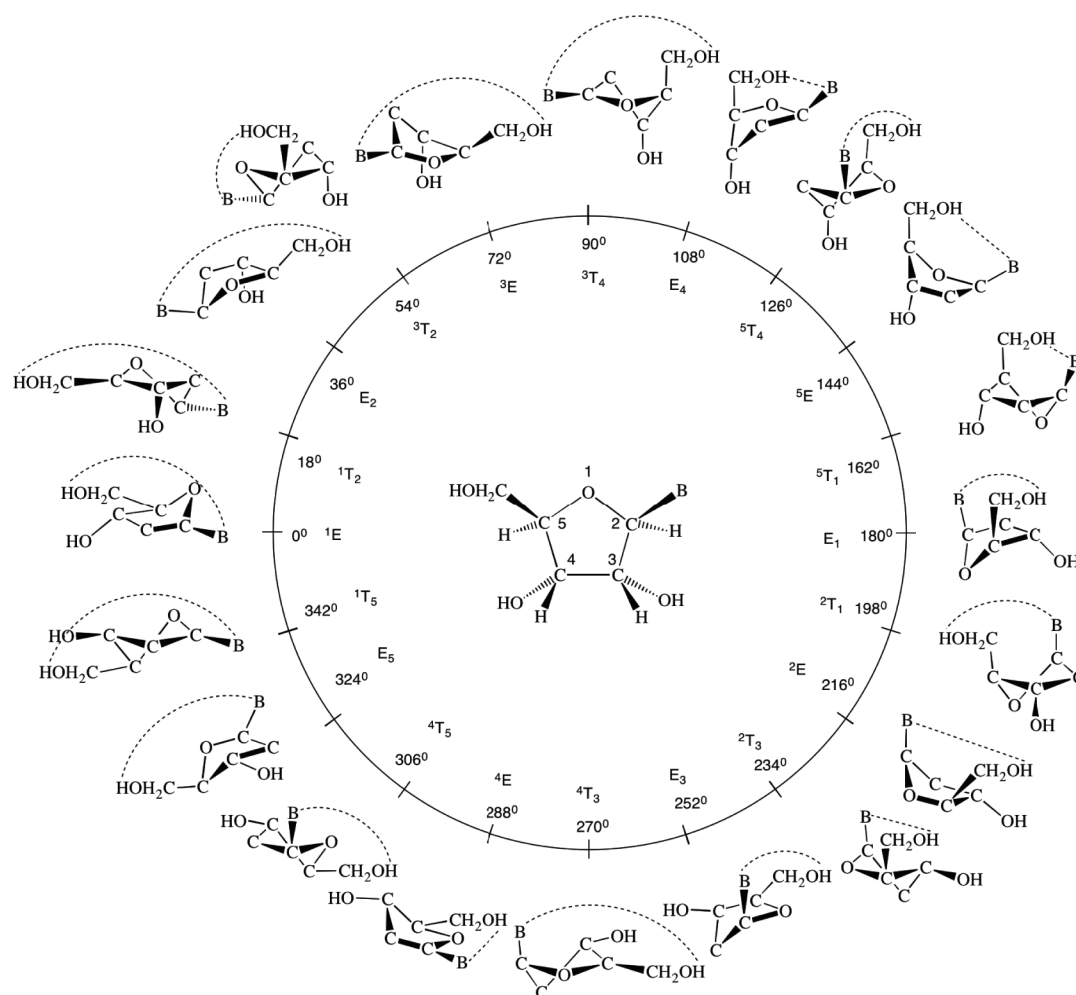
In this section, the important tools applied in this work are introduced, the Cremer–Pople ring puckering analysis,<sup>25–30</sup> the local mode analysis of Konkoli and Cremer,<sup>31–34</sup> and the topological analysis of the electron density  $\rho(r)$  via Bader's quantum theory of atoms in molecules (QTAIM) approach.<sup>35,36</sup> Then the computational details of this study are described.

**Cremer–Pople Ring Puckering Analysis.** Cremer and Pople<sup>25</sup> suggested to span the conformational space of a puckered  $N$ -membered ring with  $N - 3$  puckering coordinates. The  $N - 3$  puckering coordinates can be split up into pairs of pseudorotational coordinates  $\{q_m, \phi_m\}$  ( $m = 2, 3, \dots, N - 3$ ) for odd-membered rings and an additional puckering amplitude  $q_{N/2}$  describing ring inversion for even-membered rings. The puckering amplitude  $q_m$  describes the degree of ring puckering of the  $m$ th puckering mode. The puckering angle  $\phi_m$  defines ring puckering mode.<sup>37,38</sup> Cremer and Pople<sup>25</sup> introduced a mean plane as reference, e.g. the plane of the planar ring. The out-of-plane coordinates  $z_j$ , describing the displacement perpendicular to the mean plane can be determined by the  $N - 3$  puckering coordinate pairs  $\{q_m, \phi_m\}$ .<sup>25,37,39–41</sup> For a five-membered ring with ring atoms  $j = 1, \dots, 5$ , the out-of-plane displacements  $z_j$  for any ring conformation are given by eq 1:<sup>25,42</sup>

$$z_j = \left(\frac{2}{5}\right)^{1/2} q_2 \cos\left[\frac{4\pi(j-1)}{5} + \phi_2\right]$$

for  $j = 1, \dots, 5$  and  $\phi_2 \in [0; 2\pi]$  (1)

where the displacement  $z_j$  coordinates are normalized according to



**Figure 2.** Pseudorotational cycle ( $\phi_2 = 0^\circ \rightarrow 360^\circ$ ) of the deoxyribonucleoside sugar-ring represented by 20 conformers, (10 envelope (E) forms,  $\phi_2 = (0 + 360k)/10$  and 10 twist (T) forms  $\phi_2 = (18 + 360k)/10$ , where  $k = 0, 1, 2, \dots, 9$ ). The planar form is located at the center ( $q_2 = 0 \text{ \AA}$ ). The symbol B represents the base of the deoxyribonucleoside. The dashed line indicates the internal H-bond between the base and the  $\text{CH}_2\text{OH}$  substituent of the sugar ring.

$$\sum_{j=1}^5 z_j^2 = q_2^2 \quad (2)$$

Using puckering coordinates, the full set of  $3N - 6$  independent Cartesian coordinates of any puckered  $N$ -membered ring can be uniquely determined via  $N - 3$  puckering coordinates ( $q$  and  $\phi$ ),  $N - 3$  bond angles, and  $N$  bond lengths. Besides the out-of-plane displacement  $z_j$ , the displacements in the perpendicular  $x_j$  and  $y_j$  directions can also be specified. First, the  $z_j$  coordinates are calculated according to eq 1 (or similar formulas for  $N > 5$ );<sup>39,42</sup> then, the  $N$  bond lengths and  $N - 3$  bond angles are projected onto the mean plane of the ring. Finally, the projected ring is partitioned into segments, for which the displacements  $x_j$  and  $y_j$  are calculated according to a procedure described by Cremer.<sup>25</sup>

Although there is an infinite number of ring conformations located on a pseudorotation cycle for the sugar ring of deoxyribonucleosides, it is sufficient to investigate a representative number of conformations, as shown in Figure 2. Referring to previous work on description of tetrahydrofuran,<sup>42</sup> which is an analog to the five-membered sugar ring in deoxyribose, a subset of 20 ring conformations were optimized using a mixed set of puckering and internal coordinates. As shown in Figure 2, there

are 10 envelope (E) forms located at  $\phi_2 = (0 + 360k)/10$  (for  $k = 0, 1, 2, \dots, 9$ ) and 10 twist forms located at  $\phi_2 = (18 + 360k)/10$  (for  $k = 0, 1, 2, \dots, 9$ ). The internal H-bonds between the base and  $\text{CH}_2\text{OH}$  group of the sugar ring are indicated by a dashed line. The ring atom, which lies above the mean plane, is noted in front of the conformational symbol E/T as superscript, whereas a ring atom, which lies below the mean plane, is noted after the symbol E/T as subscript. All deoxyribonucleosides considered in this work possess  $C_1$  symmetry; therefore, the CES must also have  $C_1$  symmetry.

There are two major advantages of using ring puckering coordinates.<sup>43,44</sup> First, the geometry of the sugar ring for any given value of  $q_2$  and  $\phi_2$  can be optimized, even if this conformation does not occupy a stationary point on the CES. This would not be feasible by a description of the ring with Cartesian or internal coordinates.<sup>30</sup> For substituted ring systems such as deoxyribonucleosides, any conformer located on the CES can be uniquely described by a mixed set of puckering coordinates for the ring and internal/Cartesian coordinates for the substituents, and a physically meaningful pseudorotation path as a function of  $\phi_2$  can be obtained. The second advantage is that any property  $P$  of a puckered ring, such as energy, geometry, dipole moment, charge distribution, vibrational frequencies, or magnetic properties, can be expressed as a

Fourier series of the puckering coordinates. In the case of a five-membered ring,  $P$  takes the following general form:<sup>42</sup>

$$P(q_2, \phi_2) = \sum_{k=0}^{\infty} [P_k^c(q_2)\cos(k\phi_2) + P_k^s(q_2)\sin(k\phi_2)] \quad (3)$$

where the Fourier coefficients  $P_k^c$  and  $P_k^s$  are in turn expressed as power series in the puckering amplitude  $q_2$ :<sup>42</sup>

$$P_k(q_2) = \sum_{l=0}^{\infty} P_{kl}q_2^l \quad (4)$$

Depending on the symmetry of the ring, eq 3 can be simplified by selecting trigonometric terms. Because the puckering amplitude as well as the coefficients  $P_{kl}$  change independent of the phase angle  $\phi_2$ , the puckering amplitude  $q_2$  the Fourier coefficients can be treated as normal coefficients for further simplification. Thus, the property  $P$  can be expressed as a pure function of  $\phi_2$ , which also holds for the change of a property  $P$  along the pseudorotation path. For  $C_1$  symmetric systems eq 3 can be simplified to eq 5, which was applied in this work:

$$P(\phi_2) = \sum_{k=0}^{\infty} (A_k\cos(k\phi_2) + B_k\sin(k\phi_2)) \quad (5)$$

which according to the  $C_1$  symmetry of the deoxyribonucleosides  $\mathbf{dC}$ ,  $\mathbf{dA}$ ,  $\mathbf{dT}$ , and  $\mathbf{dG}$ , investigated in this work leads to

$$P(\phi_2) = A_0 + \sum_{i=1}^{\infty} \left( A_i\cos(i\phi_2) + \sum_{j=1}^{\infty} B_j\sin(j\phi_2) \right) \quad (6)$$

Experimentally, for a free or slightly hindered pseudorotator molecule, only a property  $\langle P \rangle$  averaged over all pseudorotational modes can be measured. Focusing exclusively on the large amplitude pseudorotational mode of the ring, the calculated property  $\langle P \rangle$  averaged over the pseudorotational motion can be determined, once the functional form of eq 6 is known, according to<sup>42</sup>

$$\langle P \rangle = \int_b^a \rho(\phi_2)P(\phi) d\phi_2 \quad (7)$$

where  $a$  and  $b$  are the boundary of pseudorotation. If  $a \neq 2\pi$  and  $b \neq 0$ , the pseudorotation is incomplete, which we call pseudolibration in reference to physics calling an incomplete rotation a libration.

The conformational probability distribution  $\rho(\phi_2)$  can be defined as a Boltzmann distribution:

$$\rho(\phi_2) = \frac{e^{-[V(\phi_2)-V(0)]/RT}}{\int_b^a e^{-[V(\phi_2)-V(0)]/RT} d\phi_2} \quad (8)$$

where  $V(\phi_2)$  is the electronic potential energy of the conformer at  $\phi_2$  on the pseudorotation path and  $V(0)$  is the electronic potential energy of planar form. The conformational probability distribution  $\rho(\phi_2)$  can be treated as a property  $P$  and, therefore, can be defined using eq 9:

$$\rho(\phi_2) = C_0 + \sum_{i=1}^{\infty} \left( C_i\cos(i\phi_2) + \sum_{j=1}^{\infty} D_j\sin(j\phi_2) \right) \quad (9)$$

The conformational probability distribution  $\rho(\phi_2)$  reflects the most likely conformers of a puckered ring on the CES.

**Local Mode Analysis.** The normal  $(3N - L)$  vibrational modes of an  $N$  atomic molecule ( $L$  is the number of translational

and rotational motions of the molecule) contain important electronic structure information and, therefore, should be well suited as a measure of bond strength. However, it is difficult to decode this information into individual atom–atom interactions (e.g., those resulting in bonding) because normal vibrational modes are generally delocalized due to the coupling of the motions of the atoms within the molecule. There are two different coupling mechanisms between vibrational modes as a consequence of the fact that there is a kinetic and a potential contribution to the energy of a vibrational mode, as reflected in the corresponding Euler–Lagrange equations  $L(\mathbf{q}, \dot{\mathbf{q}})$  for a vibrating molecule given by eq 10 in internal coordinates  $\mathbf{q}$ :<sup>31–34</sup>

$$L(\mathbf{q}, \dot{\mathbf{q}}) = \underbrace{\frac{1}{2}\dot{\mathbf{q}}^\dagger \mathbf{G}^{-1} \dot{\mathbf{q}}}_{\text{mass coupling}} - \underbrace{\frac{1}{2}\mathbf{q}^\dagger \mathbf{F}^q \mathbf{q}}_{\text{electronic coupling}} \quad (10)$$

The electronic coupling between the vibrational modes is reflected by the off-diagonal elements of the force constant matrix  $\mathbf{F}^q$ . By solving the Euler–Lagrange equations for a vibrating molecule, the basic equation of vibrational spectroscopy, e.g. the Wilson equation,<sup>45</sup> is obtained:

$$\mathbf{F}^q \mathbf{D} = \mathbf{G}^{-1} \mathbf{D} \mathbf{\Lambda} \quad (11)$$

with the diagonal matrix  $\mathbf{\Lambda}$  collecting the vibrational eigenvalues  $\lambda_\mu = 4\pi^2 c^2 \omega_\mu$  where  $\omega_\mu$  represents the harmonic vibrational frequency of mode  $\mathbf{d}_\mu$  given in reciprocal centimeters,  $c$  is the speed of light, and  $\mu = (1 \cdots N - L)$ . Solution of eq 11, e.g. diagonalizing the Wilson equation leads to the diagonal force constant  $\mathbf{K}$  given in normal coordinates  $\mathbf{Q}$  which is free of electronic coupling:

$$\mathbf{K} = \mathbf{D}^\dagger \mathbf{F}^q \mathbf{D} \quad (12)$$

Kinematic coupling or mass coupling is still present when the electronic coupling is eliminated by solving the Wilson equation. In 1998, Konkoli and Cremer<sup>31–34</sup> determined for the first time local, mass-decoupled vibrational modes  $\mathbf{a}_i$  directly from normal vibrational modes  $\mathbf{d}_\mu$  by solving the mass-decoupled Euler–Lagrange equations. The subscript  $i$  specifies an internal coordinate  $q_i$  and the local mode is expressed in terms of normal coordinates  $\mathbf{Q}$  associated with force constant matrix  $\mathbf{K}$  of eq 12. Konkoli and Cremer showed that this is equivalent to requiring an adiabatic relaxation of the molecule after enforcing a local displacement of atoms by changing a specific internal coordinate as, e.g., a bond length (*leading parameter principle*).<sup>31</sup> The local modes are unique and the local counterparts of the normal vibrational modes. They can be based on either calculated or experimentally determined vibrational frequencies via<sup>31–34,46–48</sup>

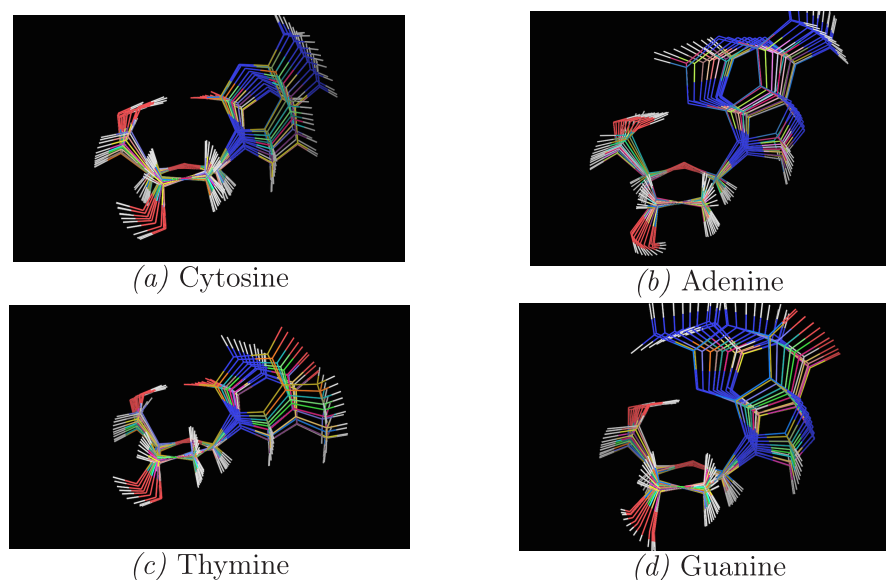
$$\mathbf{a}_i = \frac{\mathbf{K}^{-1} \mathbf{d}_i^\dagger}{\mathbf{d}_i^\dagger \mathbf{K}^{-1} \mathbf{d}_i^\dagger} \quad (13)$$

To each local mode  $\mathbf{a}_i$  a corresponding local mode frequency  $\omega_i^a$ , local mode mass  $G_{i,i}^a$  and a local force constant  $k_i^a$  can be defined.<sup>31</sup> The local mode frequencies can be uniquely connected to the normal-mode frequencies via an adiabatic connection scheme.<sup>33,34</sup> The local mode frequency  $\omega_i^a$  is defined by

$$(\omega_i^a)^2 = \frac{G_{i,i}^a k_i^a}{4\pi^2 c^2} \quad (14)$$

and the corresponding local mode force constant  $k_i^a$  by





**Figure 3.** Illustration of the 20 representative path points for each of the four deoxyribonucleosides (a) dC, (b) dA, (c) dT, and (d) dG calculated by constrained optimizations using a fixed phase angle  $\phi_2$  and increments of  $18^\circ$ , e.g.  $\phi_2 = 0, 18, 36, \dots, 342^\circ$ .

$$k_i^a = \mathbf{a}_i^\dagger \mathbf{K} \mathbf{a}_i \quad (15)$$

Local mode force constants, contrary to normal mode force constants, have the advantage of being independent of the choice of the coordinates used to describe the molecule in question and in contrast to vibrational frequencies they are independent of the atomic masses. They are extremely sensitive to differences in the electronic structure (e.g., caused by changing a substituent), and they capture only electronic effects directly associated with the intrinsic strength of the atom–atom interaction leading to a chemical bond as recently shown by Zou and Cremer.<sup>49</sup> Therefore, the local vibrational force constants provide a unique tool for assessing the strength of a chemical bond via vibrational spectroscopy, which has recently been applied to characterize strong and weak covalent bonds,<sup>49–55</sup> for the definition of new electronic parameters such as the generalized Tolman parameter<sup>56–58</sup> or a new aromaticity index.<sup>48,59–61</sup> In particular, weak chemical interactions including hydrogen, halogen, and pnictogen bonding were quantitatively assessed for the first time.<sup>62–74</sup>

In this work, we have used the local H-bond stretching frequencies  $\omega^a$  and the local stretching force constants  $k^a$  for the characterization of the strength of the intramolecular H-bonds of the deoxyribonucleosides dC, dA, dT, and dG.

It is convenient to base the comparison of the bond strength of a series of molecules on a bond strength order (BSO)  $n$  rather than on a comparison for local force constant values. Both are connected via a power relationship according to the generalized Badger rule derived by Cremer and co-workers:<sup>52,75</sup>

$$\text{BSO } n = a(k^a)^b \quad (16)$$

The constants  $a$  and  $b$  in eq 16 can be determined via two reference values and the requirement that for a zero force constant the BSO  $n$  is zero. For H-bonds,  $n = 1$  for the FH bond and  $n = 0.5$  for the FH bond in the  $[\text{F}\cdots\text{H}\cdots\text{F}]^-$  anion were used,<sup>68</sup> leading to  $a = 0.515$  and  $b = 0.291$ , (calculated at the  $\omega\text{B97X-D/6-31++G(d,p)}$  level of theory). According to eq 16 the OH bond in  $\text{H}_2\text{O}$  has a BSO  $n$  value of  $n = 0.966$ . Therefore, we scaled the reference values, so that the BSO  $n$  of the OH bond in  $\text{H}_2\text{O}$  is 1.

**QTAIM and NBO Analysis.** Bader's quantum theory of atoms in molecules (QTAIM) presents the theoretical framework for identifying and characterizing chemical bonds and weak chemical interactions via the study of the topological features of the total electron density  $\rho(r)$ .<sup>76,77</sup> In this work we used QTAIM as a complementary tool to the local mode analysis to determine the covalent/electrostatic character of internal the H-bonds via the Cremer–Kraka criterion<sup>78,79</sup> of covalent bonding. According to this criterion a covalent bond between two atoms A and B is defined by the following two conditions: (i) *Necessary condition* The existence of a bond path and bond critical point  $\mathbf{r}_c = c$  between A and B. (ii) *Sufficient condition* The energy density  $H(\mathbf{r}_c) = H_c$  is smaller than zero.  $H(\mathbf{r})$  is defined as

$$H(\mathbf{r}) = G(\mathbf{r}) + V(\mathbf{r}) \quad (17)$$

where  $G(\mathbf{r})$  is the kinetic energy density and  $V(\mathbf{r})$  is the potential energy density. The negative  $V(\mathbf{r})$  corresponds to a stabilizing accumulation of density whereas the positive  $G(\mathbf{r})$  corresponds to depletion of electron density.<sup>79</sup> As a result, the sign of  $H_c$  indicates which term is dominant.<sup>80</sup> If  $H_c < 0$ , the interaction is considered covalent in nature, whereas  $H_c > 0$  is indicative of electrostatic interactions.

We complemented the QTAIM analysis with the natural bond orbital (NBO) of Weinhold and co-workers<sup>81,82</sup> in order to obtain further insights into the intermolecular orbital interactions, particularly the charge transfer from the nitrogen/oxygen lone pair to the adjacent  $\sigma^*$  of the O–H moiety stabilizing the H-bond. Within the NBO framework the delocalization energy  $\Delta E_{\text{del}}(\text{HB})$  associated with the electron delocalization between the nitrogen/oxygen lone pair (donor) and the  $\sigma^*$  of O–H moiety (acceptor) can be estimated via the charge transfer from the localized (donor) Lewis-type orbital (L) into the empty (acceptor) non-Lewis orbital (NL)<sup>83,84</sup>

$$E^2 = \Delta E_{\text{del}}(\text{HB}) = \frac{q_L F(L, \text{NL})^2}{\epsilon_{\text{NL}} - \epsilon_L} \quad (18)$$

where  $q_L$  is the orbital and  $\epsilon_{\text{NL}}$  are the diagonal elements of the NBO Fock matrix corresponding to orbital energies of the donor orbital L and acceptor orbital NL, and  $F(L, \text{NL})$  is the off-

Table 1. Energies, Geometries, Vibrational, and Electron Density Data for Deoxyribonucleosides dA, dG, dC, and dT along Their Pseudolibration Paths<sup>a</sup>

$\phi_2$ [deg]	$q_2$ [Å]	$\Delta E$ [kcal/mol]	$\Delta G$ [kcal/mol]	R(HB) [Å]	$k^a$ (HB) [mdyn/Å]	$\omega^a$ (HB) [1/cm]	BSO $n$ (HB)	$\Delta E_{del}$ (HB) [kcal/mol]	$\omega_p(\omega^a, \text{no.}, \%)$ [1/cm]	$\rho_c$ [e/Å <sup>3</sup> ]	$H_c$ [Hartree/Å <sup>3</sup> ]	$H_c/\rho_c$ [Hartree/e]
<b>dA</b>												
270	0.256	-0.11(4.64)	-0.99(3.73)	1.866	0.226	638	0.372	20.4	130(5, 51.8)	0.232	-0.003	-0.011
288	0.304	-1.31(3.44)	-1.91(2.81)	1.909	0.152	524	0.353	18.7	130(5, 30.0), 114(4, 29.6)	0.211	-0.001	-0.006
306	0.272	-1.49(3.26)	-2.33(2.40)	1.969	0.138	499	0.330	15.4	112(4, 72.8)	0.185	-0.001	-0.005
324	0.214	-1.24(3.51)	-2.27(2.45)	1.971	0.144	510	0.329	15.6	106(4, 83.7)	0.184	-0.001	-0.004
342	0.173	-1.17(3.58)	-1.04(3.68)	1.951	0.156	531	0.337	17.2	100(4, 89.9)	0.192	-0.001	-0.004
0	0.165	-1.31(3.43)	-1.17(3.56)	1.941	0.151	523	0.341	18.2	97(4, 90.5)	0.197	-0.001	-0.004
18	0.186	-1.67(3.08)	-1.41(3.31)	1.948	0.159	536	0.338	18.2	99(4, 92.2)	0.194	-0.001	-0.003
36	0.234	-2.39(2.36)	-1.97(2.75)	1.959	0.164	544	0.333	17.9	100(4, 89.8)	0.190	-0.001	-0.004
54	0.291	-3.53(1.22)	-3.96(0.76)	1.945	0.135	493	0.339	19	98(4, 47.9), 76.3 (3, 27.9)	0.196	-0.001	-0.005
72	0.325	-4.52(0.15)	-4.64(0.09)	1.885	0.216	624	0.363	23.3	111(4, 38.7), 179(7, 28.5)	0.225	-0.002	-0.009
90	0.342	-4.68(0.07)	-4.77(-0.05)	1.826	0.249	670	0.390	28.3	182(7, 64.7)	0.258	-0.005	-0.021
108	0.343	-3.69(1.05)	-3.61(1.12)	1.784	0.326	767	0.409	32	194(7, 93.5)	0.285	-0.010	-0.034
126	0.326	-1.69(3.06)	-2.66(2.06)	1.799	0.163	543	0.411	31	6(1, 74.4)	0.288	-0.011	-0.037
<b>dG</b>												
270	0.267	-0.76(3.76)	-1.40(3.49)	1.819	0.238	655	0.377	22.7	160(7, 45.6), 128(5, 23.8)	0.262	-0.007	-0.028
288	0.308	-2.22(2.31)	-2.80(2.09)	1.862	0.187	581	0.351	20.7	162(7, 38.1), 118(4, 27.0)	0.239	-0.005	-0.020
306	0.28	-2.45(2.08)	-3.53(1.36)	1.914	0.118	462	0.323	17.5	105(4, 46.0), 69 (3, 36.9)	0.212	-0.003	-0.014
324	0.23	-2.14(2.39)	-4.94(-0.04)	1.917	0.138	498	0.321	17.8	101(4, 54.4)	0.209	-0.002	-0.011
342	0.191	-1.96(2.57)	-1.73(3.17)	1.898	0.171	556	0.331	19.8	101(4, 83.0)	0.218	-0.002	-0.011
0	0.181	-2.00(2.53)	-1.80(3.09)	1.882	0.155	528	0.340	21.6	94(4, 78.1)	0.226	-0.003	-0.011
18	0.199	-2.28(2.24)	-1.90(3.00)	1.881	0.207	611	0.340	22.4	101(4, 85.4)	0.226	-0.002	-0.010
36	0.249	-2.95(1.58)	-2.56(2.34)	1.895	0.162	541	0.333	22	6(4, 65.7)	0.219	-0.002	-0.009
54	0.306	-3.98(0.55)	-4.09(0.81)	1.879	0.223	635	0.341	23.7	117(4, 47.2), 76 (3, 41.1)	0.228	-0.002	-0.011
72	0.336	-4.53(0.00)	-4.91(-0.01)	1.827	0.229	644	0.372	28.3	75(3, 50.6)	0.257	-0.005	-0.020
90	0.334	-3.78(0.74)	-3.99(0.91)	1.768	0.327	768	0.410	34.5	186(8, 48.3), 79 (3, 35.4)	0.296	-0.011	-0.039
108	0.304	-1.79(2.73)	-2.09(2.81)	1.732	0.38	828	0.436	38.4	194(8, 41.1), 199(9, 27.3)	0.323	-0.019	-0.057
<b>dC</b>												
252	0.112	-0.17(2.95)	-1.73(1.36)	1.794	0.174	559	0.385	11.6	16(1, 56.9)	0.218	0.008	0.038
270	0.177	-0.85(2.27)	-1.71(1.38)	1.824	0.193	588	0.368	10	122(5, 65.6)	0.205	0.006	0.032
288	0.228	-1.61(1.51)	-1.96(1.13)	1.878	0.179	566	0.339	8	123(5, 73.3)	0.181	0.004	0.021
306	0.234	-1.85(1.27)	-2.38(0.70)	1.934	0.117	457	0.312	6.5	108(4, 83.4)	0.160	0.002	0.011
324	0.201	-1.51(1.61)	-2.21(0.88)	1.937	0.114	452	0.310	6.7	106(4, 93.4)	0.158	0.002	0.012
342	0.158	-1.12(2.00)	-1.10(1.99)	1.895	0.167	546	0.331	8.2	106(4, 73.2)	0.172	0.004	0.023
0	0.139	-0.91(2.21)	-0.63(2.46)	1.873	0.172	555	0.342	9.2	104(4, 79.0)	0.180	0.005	0.030
18	0.152	-0.87(2.26)	-0.63(2.46)	1.869	0.171	553	0.344	9.5	104(4, 82.1)	0.182	0.006	0.031
36	0.215	-1.15(1.98)	-0.79(2.30)	1.889	0.169	551	0.333	9	104(4, 89.9)	0.174	0.005	0.026
54	0.297	-2.13(0.99)	-2.47(0.62)	1.887	0.166	545	0.334	9.2	106(4, 84.6)	0.175	0.004	0.025
72	0.34	-3.06(0.07)	-3.08(0.01)	1.825	0.213	618	0.367	11.8	159(6, 40.6), 116(4, 33.9)	0.202	0.008	0.039
90	0.348	-2.72(0.40)	-2.64(0.45)	1.764	0.298	731	0.402	15.3	185(8, 50.5)	0.231	0.012	0.050
108	0.319	-0.88(2.24)	-1.35(1.74)	1.74	0.289	719	0.418	17.1	189(8, 91.1)	0.245	0.013	0.053
<b>dT</b>												
270	0.19	-0.79 (3.10)	-1.44 (2.31)	1.868	0.277	576	0.348	8.7	111(5, 34.4), 191(9, 21.1)	0.214	0.009	0.043
288	0.25	-1.80(2.08)	-2.29(1.46)	1.933	0.113	451	0.321	7.1	110(5, 38.4), 94 (3, 34.5)	0.162	0.002	0.011
306	0.26	-2.24(1.65)	-2.67(1.08)	2.016	0.092	405	0.290	5.4	106(4, 88.1)	0.135	0.000	0.001
324	0.228	-1.96(1.93)	-2.62(1.13)	2.028	0.089	400	0.286	5.4	102(4, 89.8)	0.131	0.000	0.001
342	0.186	-1.58(2.31)	-1.05(2.69)	1.982	0.111	446	0.303	7	102(4, 92.9)	0.143	0.001	0.007
0	0.17	-1.41(2.47)	-1.05(2.69)	1.953	0.113	450	0.313	8.4	97(4, 92.3)	0.152	0.002	0.012
18	0.186	-1.48(2.41)	-0.93(2.81)	1.948	0.127	476	0.316	9.3	100(4, 95.5)	0.153	0.002	0.014
36	0.244	-1.96(1.93)	-1.74(2.01)	1.964	0.105	433	0.309	9.7	90(4, 94.5)	0.148	0.001	0.010
54	0.313	-3.05(0.84)	-3.04(0.71)	1.947	0.137	496	0.316	11.1	104(4, 93.0)	0.154	0.002	0.011

Table 1. continued

$\phi_2$ [deg]	$q_2$ [Å]	$\Delta E$ [kcal/mol]	$\Delta G$ [kcal/mol]	$R(\text{HB})$ [Å]	$k^a(\text{HB})$ [mdyn/Å]	$\omega^a(\text{HB})$ [1/cm]	BSO $n$ (HB)	$\Delta E_{\text{del}}(\text{HB})$ [kcal/mol]	$\omega_\mu(\omega^a, \text{no.}, \%)$ [1/cm]	$\rho_c$ [e/Å <sup>3</sup> ]	$H_c$ [Hartree/Å <sup>3</sup> ]	$H_c/\rho_c$ [Hartree/e]
dT												
72	0.35	-3.86(0.02)	-3.82(-0.08)	1.873	0.188	580	0.346	14.8	108(4, 44.4), 151(6, 23.0)	0.182	0.005	0.026
90	0.353	-3.30(0.58)	-3.17(0.58)	1.8	0.277	704	0.379	19.2	174(9, 93.1)	0.214	0.009	0.043
108	0.323	-1.24(2.65)	-1.49(2.26)	1.77	0.314	750	0.394	20.5	191(9, 93.2)	0.230	0.011	0.048

<sup>a</sup>Phase angles  $\phi_2$  are in degrees; puckering amplitudes  $q_2$  are in angstroms;  $\Delta E$  and  $\Delta G$  indicate relative energy and Gibbs free energy in kilocalories per mole with respect to the planar form as reference, while the values in parentheses are relative to the global minimum as reference; bond length values  $R(\text{HB})$  are in angstroms; force constants  $k^a$  are in millidyne per angstrom; vibrational frequencies  $\omega^a(\text{HB})$  are in inverse centimeters;  $\Delta E_{\text{del}}(\text{HB})$  gives the delocalization energy of lone-pair electrons from H-bond acceptor to H-bond donor in kilocalories per mole;  $\omega_\mu(\omega^a, \text{no.}, \%)$  represents the decomposition of H-bond normal modes to local stretching mode,  $\omega^a$  is the vibrational frequency, no. is the name of normal mode given in number, and the contribution of normal mode to H-bond local stretching mode is given in percentage; electron densities  $\rho_c$  at the bond critical points are in electrons per cubic angstrom; energy densities  $H_c$  at the bond critical points are in Hartree per cubic angstrom; energy densities per electron  $H_c/\rho_c$  are in Hartree per electron. Calculated at the  $\omega\text{B97X-D/6-31++G(d,p)}$  level of theory.

diagonal NBO Fock matrix element between the L and NL orbitals. The NBO analysis was applied to all conformers located on the pseudorotation paths to determine  $\Delta E_{\text{del}}(\text{HB})$  for all internal H-bonds.

**Computational Methods.** All calculations were performed with the  $\omega\text{B97X-D}$  functional<sup>85,86</sup> and Pople's 6-31++G(d,p) basis set.<sup>87-90</sup> Tight convergence criteria were applied, (SCF iterations  $10^{-10}$  Hartree and geometry optimizations  $10^{-7}$  Hartree/Bohr) and an ultrafine grid was used for the DFT numerical integration.<sup>91</sup> First, the most stable conformer for each deoxyribonucleoside, e.g. the global minimum, was determined by fully optimizing the structures derived from all possible H-bond combinations using Cartesian coordinates. The pseudorotation path was then calculated in the following way. A puckering analysis was performed for the global minimum to obtain the corresponding phase angle  $\phi_2$  and the puckering amplitude  $q_2$ . Starting from this phase angle 20 representative path points were calculated by constrained optimizations with a fixed phase angle  $\phi_2$ , modified in increments of  $18^\circ$  for e.g.  $\phi_2 = 0, 18, 36, \dots, 342^\circ$ , as shown in Figure 3 to determine the pseudorotation path. For the constrained optimizations a mixed set of internal coordinates for the substituents and puckering coordinates for deoxyribose sugar ring was used.

Harmonic frequency calculations were carried out in each case to confirm the optimized conformers located on the pseudorotation path as minima (no imaginary frequency) or transition states (one imaginary frequency). In this regard, the pseudorotation path can be considered as a special reaction path with the phase angle  $\phi_2$  as reaction coordinate. For the lowest energy conformers being located on the opposite site of global minima, e.g. phase angles  $\phi_2$  in the range of  $\approx 300^\circ$ , a full geometry optimization was performed, to identify possible local minima, which were found for all deoxyribonucleosides in this range. For the highest energy conformers, e.g. phase angles  $\phi_2$  in the range of  $330-18^\circ$ , a full geometry optimization was performed to identify the transition state (TS) for the pseudorotation. The CESs were also mapped via constrained optimizations. For each fixed phase angle  $\phi_2$ , the puckering amplitudes  $q_2$  were constrained to four values, namely 0.1, 0.2, 0.3, and 0.4 Å, and the remainder of the molecule was optimized, leading to 80 data points for each CES. For each conformer on the pseudorotation path, a local mode analysis was performed for the investigation of the H-bond strength. Delocalization energies of the internal H-bonds were calculated for further characterization.<sup>84</sup> These energies reflect the delocalization of lone-pair electrons from H-bond acceptor to H-bond donor

The RING Puckering program<sup>26</sup> was used for analysis of the deoxyribose sugar ring conformations. For the geometry optimizations and frequency calculations, a combination of the RING Puckering program and the program package Gaussian09<sup>92</sup> was used. All local mode analyses calculations were carried out with the program package COLOGNE2019.<sup>93</sup> The NBO calculations were carried out with NBO 6.<sup>94</sup> The QTAIM analysis was performed with the AIMALL software.<sup>95</sup>

## RESULTS AND DISCUSSION

In Table 1, properties of the deoxyribonucleosides dC, dA, dT, and dG calculated at different phase angles  $\phi_2$  are listed. These comprise the puckering amplitude  $q_2$ , relative energy  $\Delta E$ , and free energy  $\Delta G$  with regard to the planar form and the global minimum, H-bond distance  $R(\text{HB})$ , force constant  $k^a(\text{HB})$ , local mode frequency  $\omega^a(\text{HB})$ , and bond strength order BSO  $n(\text{HB})$  as well the H-bond delocalization energy  $\Delta E_{\text{del}}(\text{HB})$  and the normal vibration mode(s)  $\omega_\mu$  with the highest H-bond contribution(s). Table 1 also contains the electron density  $\rho_c$  (e/Å<sup>3</sup>) and the energy density  $H_c$  (Hartree/Å<sup>3</sup>) at the bond critical point  $c$ . Table 2 summarizes H-bond properties of some

Table 2. Properties of Hydrogen Bonded Reference Complexes R1–R5<sup>a</sup>

molecule	$k^a$	BSO $n$	$R(\text{HB})$	$\rho_c$	$H_c$	$H_c/\rho_c$
R1	0.209	0.360	1.905	0.183	-0.001	-0.005
R2	0.214	0.362	1.895	0.176	0.002	0.012
R3	0.044	0.241	2.457	0.071	0.003	0.048
R4	0.116	0.309	1.981	0.162	-0.004	-0.027
R5	0.205	0.358	1.922	0.202	0.000	0.002

<sup>a</sup>Force constants  $k^a$  are in millidyne per angstrom; H-bond lengths  $R(\text{HB})$  are in angstroms,  $\rho_c$  values are in electrons per cubic angstrom;  $H_c$  values are in Hartree per cubic angstrom; energy densities per electron  $H_c/\rho_c$  are in Hartree per electron. Reference complexes R1–R5 are shown in Figure 9. Calculated at the  $\omega\text{B97X-D/6-31++G(d,p)}$  level of theory.

reference molecules. In Table 3, geometric features, including  $R(\text{HB})$ , angles  $\alpha_1$  and  $\alpha_2$ , and dihedral angles  $\tau_1$  and  $\tau_2$  between the base and the CH<sub>2</sub>OH group forming the intramolecular H-bond of the conformer with the strongest H-bond ( $\phi_2 = 108^\circ$ ), and that with the weakest H-bond ( $\phi_2 = 324^\circ$ ) are summarized for puckering amplitude values of 0.1, 0.2, 0.3, and 0.4 Å.

**CESs and Pseudorotation (Pseudolibration) Paths.** The pseudorotation paths on the corresponding CESs the

Table 3. Geometric Features of Conformers at  $\phi_2 = 108^\circ$  (Region of Strongest H-Bonds) and  $\phi_2 = 324^\circ$  (Region of Weakest H-Bonds)<sup>a</sup>

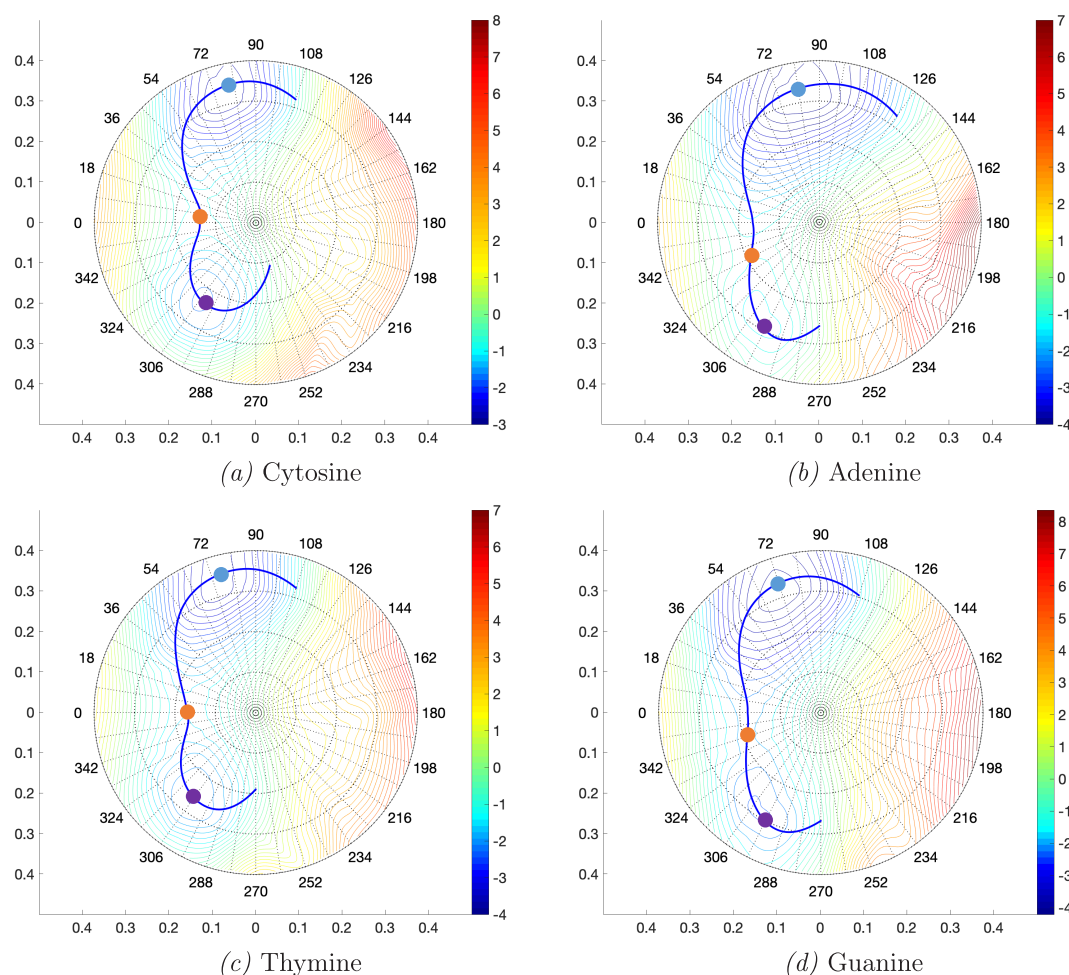
	$q_2$ [Å]	$r(\text{HB})$ [Å]	$\alpha_1$ [deg]	$\alpha_2$ [deg]	$\tau_1$ [deg]	$\tau_2$ [deg]	$\sum(\alpha_1, \alpha_2)$ [deg]	$\Delta(\tau_1, \tau_2)$ [deg]	$\Delta E$ [kcal/mol]
<b>dA</b>									
$\phi_2 = 108^\circ$	0.1	1.800	23.9	32.2	54.8	-93.5	56.1	38.6	-0.76
	0.2	1.784	21.9	36.4	55.7	-93.4	58.4	37.7	-2.25
	0.3	1.783	20.3	40.0	56.8	-93.4	60.3	36.7	-3.52
	0.4	1.787	18.7	42.9	57.0	-92.2	61.6	35.2	-3.34
$\phi_2 = 324^\circ$	0.1	1.872	25.7	23.7	51.3	-89.1	49.4	37.8	-0.74
	0.2	1.929	25.4	20.0	49.0	-86.5	45.4	37.5	-1.22
	0.3	1.988	24.9	16.8	47.6	-85.3	41.8	37.7	-0.78
	0.4	2.073	23.4	13.6	56.4	-85.6	36.9	29.2	1.21
<b>dG</b>									
$\phi_2 = 108^\circ$	0.1	1.747	23.2	30.9	64.3	-81.7	54.2	17.4	-0.23
	0.2	1.732	21.4	35.4	64.6	-83.0	56.7	18.4	-1.15
	0.3	1.732	19.7	39.2	65.2	-83.2	58.9	18.0	-1.79
	0.4	1.735	18.0	42.3	65.4	-82.0	60.3	16.6	-0.85
$\phi_2 = 324^\circ$	0.1	1.825	25.1	21.9	60.8	-77.1	47.0	16.3	-1.29
	0.2	1.893	24.7	18.0	57.9	-75.7	42.7	17.8	-2.09
	0.3	2.000	24.3	14.3	55.4	-76.0	38.6	20.6	-1.72
	0.4	2.201	23.6	10.8	54.4	-77.9	34.3	23.5	0.50
<b>dC</b>									
$\phi_2 = 108^\circ$	0.1	1.759	23.6	30.9	63.6	-97.7	54.5	34.1	0.34
	0.2	1.742	21.1	35.2	64.8	-97.9	56.4	33.1	-0.19
	0.3	1.738	19.1	39.1	64.7	-97.8	58.2	33.1	-0.85
	0.4	1.750	17.3	42.3	63.4	-97.1	59.5	33.6	-0.25
$\phi_2 = 324^\circ$	0.1	1.837	25.5	22.9	59.9	-91.1	48.4	31.2	-1.04
	0.2	1.937	24.8	19.5	58.6	-87.8	44.3	29.2	-1.51
	0.3	2.128	23.8	16.4	58.2	-86.7	40.2	28.6	-0.91
	0.4	2.672	22.1	12.9	62.7	-88.5	35.0	25.8	0.90
<b>dT</b>									
$\phi_2 = 108^\circ$	0.1	1.789	23.6	31.4	60.8	-98.3	55.0	37.5	0.20
	0.2	1.773	21.2	35.6	62.1	-98.6	56.7	36.5	-0.45
	0.3	1.768	19.2	39.3	61.5	-98.9	58.5	37.4	-1.20
	0.4	1.779	17.5	42.4	60.3	-98.5	59.8	38.2	-0.65
$\phi_2 = 324^\circ$	0.1	1.878	25.5	23.5	56.6	-92.2	49.1	35.6	-1.20
	0.2	1.986	24.9	20.2	54.7	-89.2	45.1	34.5	-1.91
	0.3	2.198	24.1	17.3	54.5	-88.0	41.3	33.5	-1.65
	0.4	2.811	22.4	14.1	59.6	-89.7	36.5	30.1	-0.30

<sup>a</sup> $\phi_2 = 108^\circ$  corresponds to the envelope form E<sub>4</sub> and  $\phi_2 = 324^\circ$  corresponds to the envelope form E<sub>5</sub>; see Figure 2.  $\sum(\alpha_1, \alpha_2)$  is the sum of angles  $\alpha_1$  and  $\alpha_2$ .  $\Delta(\tau_1, \tau_2)$  is the difference of  $|\tau_2| - \tau_1$ .  $\Delta E$  is the conformational energy with regard to the planar form. Calculated at the  $\omega\text{B97X-D/6-31+G(d,p)}$  level of theory.

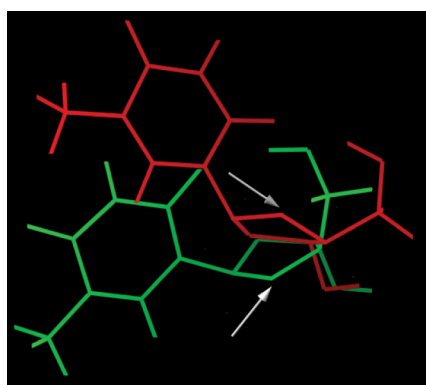
deoxyribonucleosides **dC**, **dA**, **dT**, and **dG** are shown in Figure 4. We found on the pseudorotation paths of all deoxyribonucleosides negative puckering amplitudes in the range of  $\phi_2 = 108$  to  $270^\circ$  indicating a ring inversion. As an example, the ring inversion for **dT** is shown in Figure 5 for conformer 1 (green color) with  $\phi_2 = 108^\circ$  and  $q_2 = +0.323$  Å and conformer 2 (red color) with  $\phi_2 = 144^\circ$  and  $q_2 = -0.228$  Å. This inversion leads to an incomplete pseudorotation, i.e. the pseudorotation path is not a closed circle as expected (see Figure 2) but an open curve, which we coined as pseudolibration path. As discussed in the Supporting Information for **dA** as an example, the energies beyond the ring inversion point are higher than the energy of the planar form, and as such there is no longer a minimum energy path on the CES. This suggests that when the deoxyribonucleoside reaches the end-point of the path (e.g., ring inversion point) during a thermal motion, it prefers to return back to the energetically lower part of CES via the pseudolibration path instead of entering the high energy regions.

On each of the pseudolibration paths a global minimum in the range of  $\phi_2 = 72$ – $90^\circ$  and a local minimum in the range of  $\phi_2 = 306^\circ$  separated by a transition state in the range of  $\phi_2 = 18$ – $342^\circ$  was identified, as shown in Figure 4. Energy differences  $\Delta E$  between the global and local minima are 3.24, 2.05, 1.26, and 1.65 kcal/mol, respectively for **dA**, **dG**, **dC** and **dT**; see also Table 1. The puric bases (**dA** and **dG**) process somewhat larger  $\Delta E$  values compared to the pyrimidic bases (**dC** and **dT**) which is also reflected by the fact that the former possess longer pseudolibration paths, i.e., they are conformationally more flexible. The transition states for the pseudolibration are located at  $\phi_2 = 337.7^\circ$ ,  $347.5^\circ$ ,  $13.5^\circ$ , and  $4.7^\circ$  for **dA**, **dG**, **dC**, and **dT**. The corresponding pseudolibration barriers from the global minimum to the local minimum are 3.59, 2.58, 2.26, and 2.48 kcal/mol for **dA**, **dG**, **dC**, and **dT**. The reverse barriers, e.g. from local minimum to global minimum, are only 0.34, 0.53, 1, and 0.84 kcal/mol; see Table 1.





**Figure 4.** Conformational energy surfaces (CESs) and pseudolibration paths of deoxyribonucleosides **dC** (a); **dA** (b); **dT** (c); and **dG** (d). At the center of each CES, the planar deoxyribose ring form is located. The corresponding energy is used as reference. Both  $x$  and  $y$  axes show the magnitude of puckering amplitude  $q_2$  in angstroms. The outer radius of the CES represents the maximum puckering amplitude of 0.4 Å. The labels around the CES circle denote the value of the phase angle  $\phi_2$  in degrees. The solid blue line indicates the pseudolibration path. The color bar represents the energy on the CES in kilocalories per mole relative to the planar form: (yellow to red regions) location of conformers higher in energy than the planar form; (green to blue regions) location of conformers lower in energy than the planar form. The blue dot in the range 72–90° shows the location of the global, the purple dot near 306° shows the location of the local minimum, and the yellow dot in the range 18–342° shows the transition state between the two forms. Calculated at the  $\omega$ B97X-D/6-31++G(d,p) level of theory.

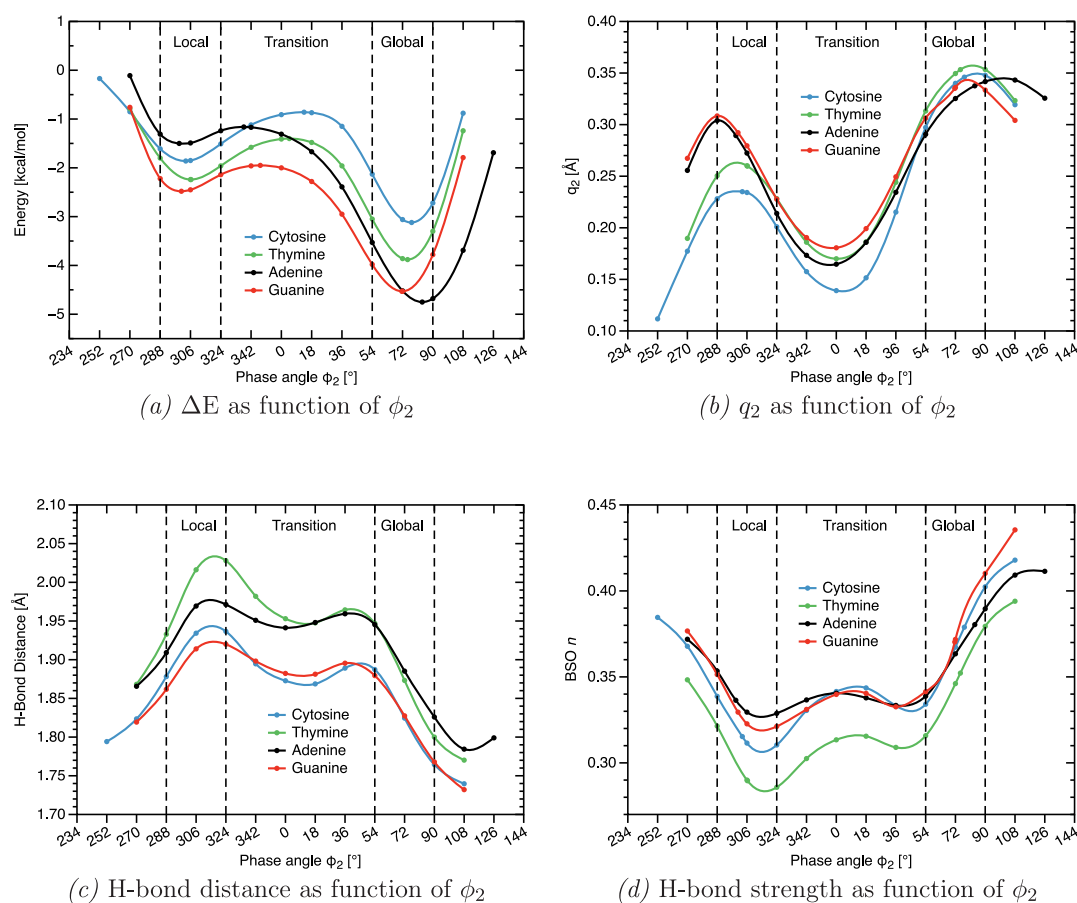


**Figure 5.** Ring inversion of the sugar ring (marked by silver arrows) of **dT**; conformer 1 is shown in green,  $\phi_2 = 108^\circ$  and  $q_2 = +0.323$  Å, and conformer 2 is shown in red,  $\phi_2 = 144^\circ$  and  $q_2 = -0.228$  Å.

More detailed information is obtained by plotting changes of  $\Delta E$ ,  $q_2$ ,  $R(\text{HB})$ , and BSO  $n(\text{HB})$  as a function of  $\phi_2$  as shown in Figure 6. The pseudolibration paths can be divided into three

distinct regions; (1) *Global minimum region*: including all conformers  $n$  with an energy difference  $\Delta E = (E_n - E_{\text{global}})$  less than 1.0 kcal/mol. For all deoxyribonucleosides, this region covers  $\phi_2$  angles in the range of 54–90°. (2) *Local minimum region*: including all conformers  $m$  with an energy difference  $\Delta E = (E_m - E_{\text{local}})$  less than 0.5 kcal/mol. For all deoxyribonucleosides, this region covers  $\phi_2$  angles in the range of 288–324°. (3) *Transition region*: Including all conformers in between, e.g.  $\phi_2$  angles in the range of 342–36°; see Figure 6. All conformers located either in the global or minimum region were identified to have no imaginary frequencies. All other conformers in the transition region and the regions outside the global and local minima ( $\phi_2$  angles in the range of 234–270° and 108–144°) were identified to have one imaginary frequency.

A comparison of Figure 6a and b reveals how the puckering amplitude and the conformational energy are related. All deoxyribonucleosides feature the same deoxyribose ring puckering pattern: the strongest puckering occurs in the global minimum region ( $\phi_2 = 72\text{--}90^\circ$ ,  $q_2$  values up to 0.35 Å), followed by the puckering in the local minimum region ( $\phi_2 =$

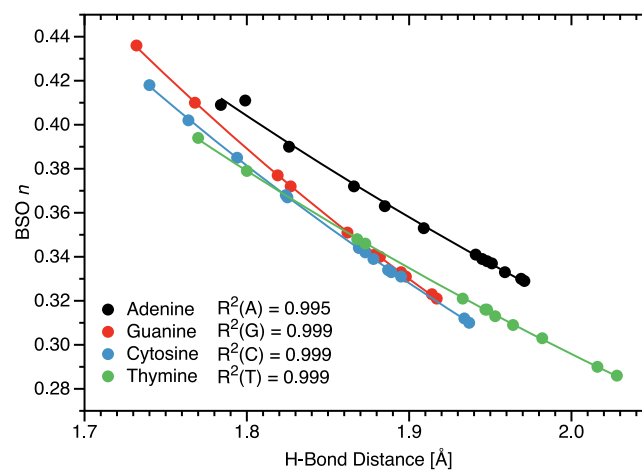


**Figure 6.** (a) Changes of the conformational energy  $\Delta E$  with regard to the planar form, (b) puckering amplitude  $q_2$ , (c) H-bond distance  $R(\text{HB})$ , and (d) H-bond strength order BSO  $n$  along the pseudolibration path described as a function of the puckering angle  $\phi_2$ . The local minimum, transition, and global minimum regions are denoted by vertical dashed lines. For a definition of these regions, see the text. Calculated at the  $\omega\text{B97X-D}/6\text{-31++G(d,p)}$  level of theory.

288–306°,  $q_2$  values up to 0.31 Å), while the smallest puckering ( $q_2 = 0.15\text{--}0.18$  Å) occurs in the transition region in the range of  $\phi_2 = 324\text{--}54^\circ$ , suggesting that the larger the puckering amplitude, the lower the conformational energy. This holds for the pyrimidic bases **dC** and **dT** for which the energy and amplitude curves are perfect mirror images, e.g. smallest amplitude values correspond to highest energy values. The puckering amplitude curves of the puric bases **dA** and **dG** are almost identical in the local energy region, whereas the difference in the conformational energy is up to 1 kcal/mol. This shows that there are additional factors determining the conformational energy, such as constrained flexibility via H-bonding which in turn can be different for the different bases.

Figure 6c and d shows the change of the internal H-bond distance  $R(\text{HB})$  and the corresponding H-bond strength BSO  $n$  along the pseudolibration path. There is a direct relationship between H-bond length and strength, i.e. the strongest H-bonds are the shortest as also reflected by Figure 7. This is not always true as numerous examples have shown.<sup>96,97</sup> Figure 7 reveals that there is a considerable variation in the H-bond lengths (0.334 Å) leading to H-bond strength differences of 0.15.

There is no obvious correlation between the H-bond length/strength and the conformational energy change. The longest and weakest H-bonds are found in the local minimum region for all deoxyribonucleosides, with the longest H-bond of 2.028 Å at  $\phi_2 = 324^\circ$  for **dT** compared with 1.917 Å at  $\phi_2 = 324^\circ$  for **dG**. If the H-bond strength would dominate the conformational energy,

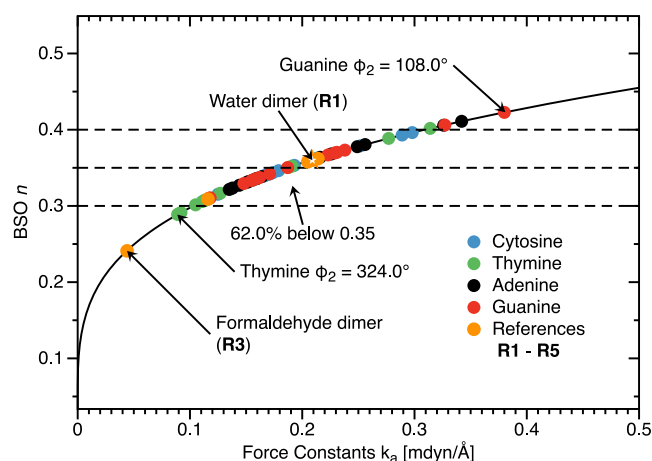


**Figure 7.** Correlation between H-bond strength and H-bond length. Calculated at the  $\omega\text{B97X-D}/6\text{-31++G(d,p)}$  level of theory.

according to Figure 6a the longest H-bonds should be located in the transition region and at the end points of the pseudolibration paths. However, we find for all deoxyribonucleosides smallest BSO  $n$  values at the end of local minimum region ( $\phi_2 = 306\text{--}324^\circ$ ) which increase through the transition region to the global minimum region ( $\phi_2 = 54\text{--}90^\circ$ ). However, the shortest and strongest H-bonds are located outside both the global minimum region (1.732 Å at  $\phi_2 = 108^\circ$  for **dG**) and the local minimum

region (1.794 Å at  $\phi_2 = 252^\circ$  for **dC**), i.e. at the turning points of the pseudolibration path, where the deoxyribonucleosides bounce back into the opposite path direction. These results clearly reveal that H-bonding determines the shape and length of the pseudolibration paths.

**Internal H-Bond Strength and Covalent/Electrostatic Character.** The weakest H-bond (BSO  $n = 0.286$ ) is found for the **dT** conformer at  $\phi_2 = 324.0^\circ$  which is still stronger than the H-bond in the formaldehyde dimer **R3**, (BSO  $n = 0.241$ , see Table 2). The **dG** conformer at  $\phi_2 = 108.0^\circ$  has the strongest H-bond (BSO  $n = 0.436$ )—see Figure 8—which is even stronger

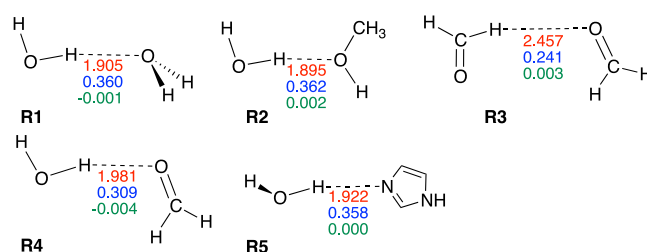


**Figure 8.** Bond strength BSO  $n$  of the H-bonds of all deoxyribonucleoside conformers as a function of the corresponding local stretching force constant  $k^a$  as determined via eq 16. For comparison H-bonded complexes **R1–R5** defined in Figure 9 are included. Dashed horizontal lines mark BSO  $n$  values of 0.3, 0.35, and 0.4, respectively. Calculated at the  $\omega$ B97X-D/6-31++G(d,p) level of theory.

than the H-bond in the water dimer **R1** with a BSO  $n$  value of 0.360; see Table 2. The percentage of conformers with BSO  $n$  values between 0.3 and 0.35 is 62.0%, in the range of the most common H-bond types in water clusters.<sup>68</sup> This clearly shows that the intermolecular H-bonds are of considerable strength and that they are an important feature of deoxyribonucleosides.

In addition to the H-bond strength we evaluated the covalent/electrostatic character of the H-bonds applying the Cremer–Kraka criterion of covalent bonding<sup>78–80,98</sup> described above. As reflected by data in Table 1  $H_c/\rho_c$  values range from  $-0.057$  Hartree/e (covalent character) for **dG** at the  $\phi_2 = 108^\circ$  turning point (strongest H-bond, BSO  $n = 0.436$ ) to  $0.053$  Hartree/e (electrostatic character) for **dC** again at the  $\phi_2 = 108^\circ$  turning point (second strongest H-bond, BSO  $n = 0.418$ ). Similar values were also found for the H-bonds of the reference compounds **R1–R5** shown in Figure 9 as revealed by the data in Table 2. These  $H_c/\rho_c$  magnitudes are typical of H-bonding<sup>99</sup> and small compared with the corresponding values for the OH bond in  $H_2O$  ( $-1.666$  Hartree/e) and the H-donor bond in **R1** ( $-1.689$  Hartree/e).<sup>68,100,101</sup>

In Figure 10a normalized energy density  $H_c/\rho_c$  values are correlated with the amplitudes  $q_2$  for all conformers of the four deoxyribonucleosides. As expected there is no general relationship because the amplitude  $q_2$  is a more global property reflecting complex geometry changes induced by ring puckering while  $H_c/\rho_c$  is taken only at a single point. However, one finds a clear separation into puric and pyrimidic bases caused by the different sign of the corresponding  $H_c/\rho_c$  values. In Figure 10b,



**Figure 9.** Reference complexes **R1–R5**. The intramolecular H-bond distance (Å) is given in red, the corresponding BSO  $n$  value is in blue, and energy density  $H_c$  (Hartree/Å<sup>3</sup>) is in green. Calculated at the  $\omega$ B97X-D/6-31++G(d,p) level of theory.

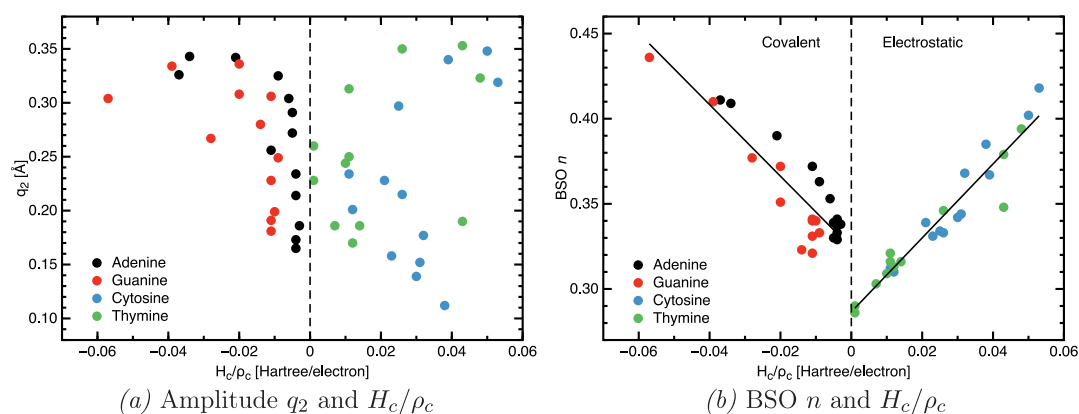
BSO  $n$  values are correlated with  $H_c/\rho_c$ . There is no overall relationship between BSO  $n$  and  $H_c/\rho_c$  for all conformers. However, there is a correlation between BSO  $n$  and  $H_c/\rho_c$  for the puric bases **dA** and **dG** as well as for the pyrimidic bases **dC** and **dT**. Larger BSO  $n$  values correspond to larger  $H_c/\rho_c$  magnitudes in both cases.

The finding that **dA** and **dG** conformers possess negative  $H_c/\rho_c$  values, i.e. being located on the covalent side of Figure 10, whereas all **dC** and **dT** conformers possess positive  $H_c/\rho_c$ , i.e. being located on the electrostatic side of Figure 10, which reflects the influence of the base determining (i) the different H-bond type, [O–H...N] for the puric bases and [O–H...O] bonds for the pyrimidic bases, and (ii) leading to a different electronic environment, i.e. in the more bulky puric bases the electron density can delocalize more than in the pyrimidic bases influencing the lone pair density of the H-bond acceptor atom. This will be discussed in more detail in the following.

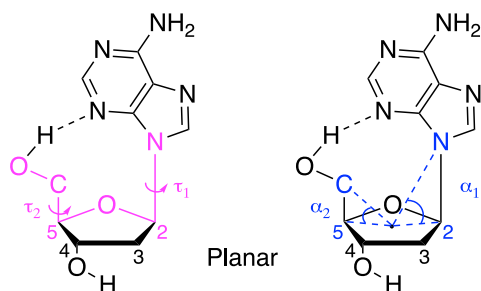
**Influence of the Orientation of the CH<sub>2</sub>OH Group and the Base on H-Bonding.** As discussed above (see Figure 7) there is a correlation between H-bond distance and H-bond strength for all four deoxyribonucleosides, but no obvious correlation between the conformational energy and H-bond distance, in particular in the local and transition region, (see Figure 6a and c), which needs further analysis. The H-bond distance depends on the mutual orientation of the CH<sub>2</sub>OH substituent (*H-bond donor*) of the C5 sugar ring carbon and the base (*H-bond acceptor*) attached to the C2 sugar ring carbon, which in turn depends on the ring pucker. This mutual orientation is also critical for optimal orbital overlap, i.e. the O–H should point to the lone pair of the H-bond acceptor atom A (A = N for **dA**, **dG**; A = O for **dC**, **dT**) in a way that the angle (OHA) is close to  $180^\circ$ .<sup>101</sup>

For the quantification of this orientation we used two torsion angles, defined in Figure 11; torsion angle  $\tau_1$  describing the rotation of the base and torsion angle  $\tau_2$  describing the rotation of the CH<sub>2</sub>OH group perpendicular to the sugar ring. The dihedral difference  $\Delta(\tau_1, \tau_2) = |\tau_2| - \tau_1$  can serve as measure of the distance between H-bond donor and acceptor; i.e. smaller dihedral differences indicate shorter H-bonds and in this way stronger H-bonds. For the global minimum geometries the dihedral differences  $\Delta(\tau_1, \tau_2)$  are  $24.3^\circ$ ,  $1.3^\circ$ ,  $13.1^\circ$ , and  $16.3^\circ$  for **dA**, **dG**, **dC**, and **dT**, respectively. For the local minimum geometries  $\Delta(\tau_1, \tau_2)$  are larger with values of  $43.1^\circ$ ,  $25.1^\circ$ ,  $33.8^\circ$ , and  $39.1^\circ$  for **dA**, **dG**, **dC**, and **dT**, respectively. This reveals that for the global minimum geometries H-bond interactions are stronger. The largest difference between the global and the local minimum  $\Delta(\tau_1, \tau_2)$  values are found for **dG** ( $23.8^\circ$ ), followed by **dT** ( $22.8^\circ$ ), **dC** ( $20.7^\circ$ ), and **dA** ( $18.8^\circ$ ). Obviously, in the local minimum region, i.e. for puckering angles  $\phi_2$  between  $288^\circ$  and





**Figure 10.** (a) Correlation between amplitude  $q_2$  and normalized energy density  $H_c/\rho_c$ . (b) Correlation of BSO  $n$  and normalized energy density  $H_c/\rho_c$ . Calculated at the  $\omega$ B97X-D/6-31++G(d,p) level of theory.



**Figure 11.** Definition of torsion angles  $\tau_1$  and  $\tau_2$  (pink color) and angles  $\alpha_1$  and  $\alpha_2$  (blue color) as listed in Table 3.

$324^\circ$  the  $\text{CH}_2\text{OH}$  group and the base cannot orient in an optimal way.

Besides a rotational movement the substituents can tilt relative to the main plane of the deoxyribose ring described by angles  $\alpha_1$  and  $\alpha_2$  for the base and the  $\text{CH}_2\text{OH}$  group respectively, as shown in Figure 11. For the global minimum geometries the tilting angle  $\alpha_2$  of the  $\text{CH}_2\text{OH}$  adapts values of  $37.1^\circ$ ,  $34.1^\circ$ ,  $35.6^\circ$ ,  $35.3^\circ$  for **dA**, **dG**, **dC**, and **dT**, respectively. For the local minimum geometries  $\alpha_2$  values are smaller:  $17.3^\circ$ ,  $14.6^\circ$ ,  $18.3^\circ$ , and  $18.3^\circ$  for **dA**, **dG**, **dC**, and **dT**, respectively. The tilting angles  $\alpha_1$  of the base are  $15.2^\circ$ ,  $13.3^\circ$ ,  $12.4^\circ$ , and  $12.1^\circ$  for the global minimum geometries and  $29.0^\circ$ ,  $29.1^\circ$ ,  $28.0^\circ$ , and  $27.8^\circ$  for the local minimum geometries of **dA**, **dG**, **dC**, and **dT**, respectively. The sum  $\sum(\alpha_1, \alpha_2)$  of the tilting angles  $\alpha_1$  and  $\alpha_2$  reflects the distance between H-bond donor and acceptor. The larger the sum  $\sum(\alpha_1, \alpha_2)$ , the smaller the distance between the H-bond donor and acceptor and the stronger is the H-bond. For the puric bases, the differences of  $\sum(\alpha_1, \alpha_2)$  between the global and local minimum geometries are  $6.1^\circ$  and  $3.6^\circ$  for **dA** and **dG**, respectively. The corresponding differences for the pyrimidic bases are somewhat smaller with  $1.7^\circ$  and  $1.4^\circ$  for **dC** and **dT**, respectively. This indicates that the tilting movement is more pronounced for the puric bases although they are more bulky than their pyrimidic counterparts. Overall, our analysis suggests that side group rotation is more important for the H-bond formation than tilting.

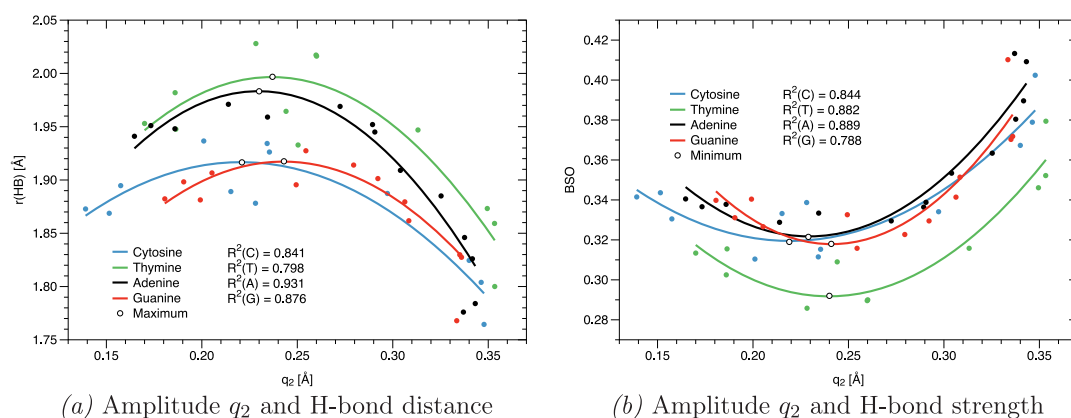
The strength of the H-bond also depends on the orientation and electron density distribution of the lone pair of the H-bond acceptor atom (N, respectively O). Both can be assessed via the delocalization energy  $\Delta E_{\text{del}}(\text{HB})$  as defined in eq 18. The larger  $\Delta E_{\text{del}}(\text{HB})$ , the stronger the H-bond.<sup>83,84</sup> As revealed by the data in Table 1 larger  $\Delta E_{\text{del}}$  values along the pseudorotation

paths are found for the puric bases **dA** and **dG** than for the pyrimidic bases **dC** and **dT**.  $\Delta E_{\text{del}}$  values for the pyrimidic bases at the global minima are  $32.0 \text{ kcal/mol}$  ( $\phi_2 = 108^\circ$ ,  $q_2 = 0.343 \text{ \AA}$ ) for **dA** and  $38.4 \text{ kcal/mol}$  ( $\phi_2 = 108^\circ$ ,  $q_2 = 0.304 \text{ \AA}$ ) for **dG**, compared to the pyrimidic bases,  $17.1 \text{ kcal/mol}$  ( $\phi_2 = 108^\circ$ ,  $q_2 = 0.319 \text{ \AA}$ ) for **dC** and  $20.5 \text{ kcal/mol}$  ( $\phi_2 = 108^\circ$ ,  $q_2 = 0.323 \text{ \AA}$ ) for **dT**. This is in line with the finding that puric bases generally tend to have a more delocalized electron density than pyrimidic bases<sup>102</sup> inducing a more delocalized electron density at the lone pair of the H-bond acceptor atom and in this way leading to stronger H-bonding. This is in line with our finding that H-bonding in the puric bases is of more covalent nature and that the global minimum conformation of **dG** has the strongest H-bond of all conformers investigated in this work with a BSO  $n$  value of 0.436.

In order to gain additional insights into these important side group effects and for better comparison, we evaluated torsion and tilting angles for all deoxyribonucleosides for the same two puckering modes,  $\phi_2 = 108^\circ$  and  $\phi_2 = 324^\circ$  (envelope forms  $E_4$  and  $E_5$ , respectively, see Figure 2), corresponding to strong and weak H-bond regions and for four different amplitudes 0.1, 0.2, 0.3, and  $0.4 \text{ \AA}$  mapping the angle changes along the CES; see Table 3. As suggested by the pseudorotation cycle shown in Figure 2, ring puckering for the  $\phi_2 = 108^\circ$  conformation should allow a better interaction between the  $\text{CH}_2\text{OH}$  group and the base than that for  $\phi_2 = 324^\circ$ .

According to the data in Table 3 for puckering mode  $E_4$ ,  $\alpha_1$  is decreasing whereas  $\alpha_2$  is increasing for increasing puckering amplitudes for all deoxynucleosides. These two opposite movements balance each other, so that as a consequence, the  $\sum(\alpha_1, \alpha_2)$  is increasing to  $61.6^\circ$ ,  $60.3^\circ$ ,  $59.5^\circ$ , and  $59.8^\circ$  for **dA**, **dG**, **dC**, and **dT**, respectively, reflecting strong H-bonding. It is also noteworthy, that the effect is almost similar for all deoxyribonucleosides quantifying the trends shown in Figure 6. In contrast, for puckering mode  $E_5$  both  $\alpha_1$  and  $\alpha_2$  are decreasing for increasing amplitudes, so that the  $\sum(\alpha_1, \alpha_2)$  is also decreasing to  $36.9^\circ$ ,  $34.3^\circ$ ,  $35^\circ$ , and  $36.5^\circ$  for **dA**, **dG**, **dC**, and **dT**, respectively, reflecting weak H-bonding. In addition, the decreasing values of both tilting angles indicate that the equatorial position is more favorable when the ring puckers with a larger amplitude. As shown in Table 3 overall changes in  $\Delta(\tau_1, \tau_2)$  for increasing puckering amplitudes are somewhat less pronounced. Overall this analysis shows that both the puckering amplitude and the puckering mode have a substantial influence on H-bond formation.





**Figure 12.** (a) Correlation of puckering amplitude  $q_2$  and H-bond distance, (b) correlation of puckering amplitude  $q_2$  and H-bond strength, expressed as a quadratic function of the puckering amplitude  $q_2$ . The color points indicate the original calculated data. The lines represent the corresponding H-bond property as a quadratic function of  $q_2$ . The curve maxima (a) and minima (b) are denoted by open circles. Calculated at the  $\omega$ B97X-D/6-31++G(d,p) level of theory.

### Interplay of Ring Puckering and Internal H-Bonding.

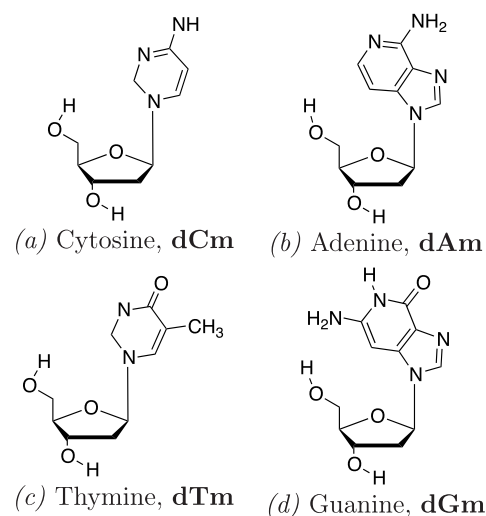
In the following it will be discussed how the puckering amplitude  $q_2$  is related to the H-bond length/strength. As shown in Figure 12, there is a qualitative quadratic relationship between the two quantities.

An increase of the puckering amplitude  $q_2$  first leads to an increase of the H-bond length (Figure 12a) reaching a maximum value around  $q_2 = 0.25$  Å, followed by a decrease of the H-bond length for larger puckering amplitudes. This corresponds to a decrease of the H-bond strength, reaching a minimum value around  $0.25$  Å, followed by an increase of the bond strength (Figure 12b). This is in line with Figure 6c revealing that at the local minima on the CESs located around the puckering angle  $\phi_2 = 306^\circ$  with puckering amplitudes  $q_2$  in the range of  $0.23$  and  $0.27$  Å (see Figure 6b) the longest H-bonds are found. After passing through the local minima, the H-bond distances decrease until reaching minimum values beyond the global minima at the turning points of the pseudolibration paths. This implies that the H-bond strength increases along the pseudolibration path from the local minimum, through the transition state, to the global minimum on CES and beyond as a result of ring puckering, clarifying that there is no direct relationship between the conformational energy and the H-bond length/strength, which would have implied longest/weakest H-bonds in the transition region.

### Comparison with H-Bond Free Model Analogues.

Finally we studied the four H-bond free deoxyribonucleosides analogs **dmC**, **dmA**, **dmT**, and **dmG** shown in Figure 13 in order to determine (i) if the pseudolibration path on the CES surface converts into a full pseudorotation path if the H-bonding is eliminated and (ii) if there is still a global and local minimum separated by a transition state.

The CESs of the H-bond free analogs are shown in Figure 14. For all analogs there exists still a pseudolibration path, which for the pyrimidic bases **dCm** and **dTm** is considerably longer compared with their original counterparts. That means that removal of the H-bond does not restore the full conformational flexibility of the sugar ring. We still find global and local minima separated a transition state on the CESs of **dCm** and **dTm** (see Figure 14a and c). However, without the influence of the internal H-bond, the transition region shrinks from  $\phi_2 = 342^\circ - 36^\circ$  to  $\phi_2 = 342^\circ - 18^\circ$  and the position of local and global minima are exchanged. In the case of the puric bases **dAm** and



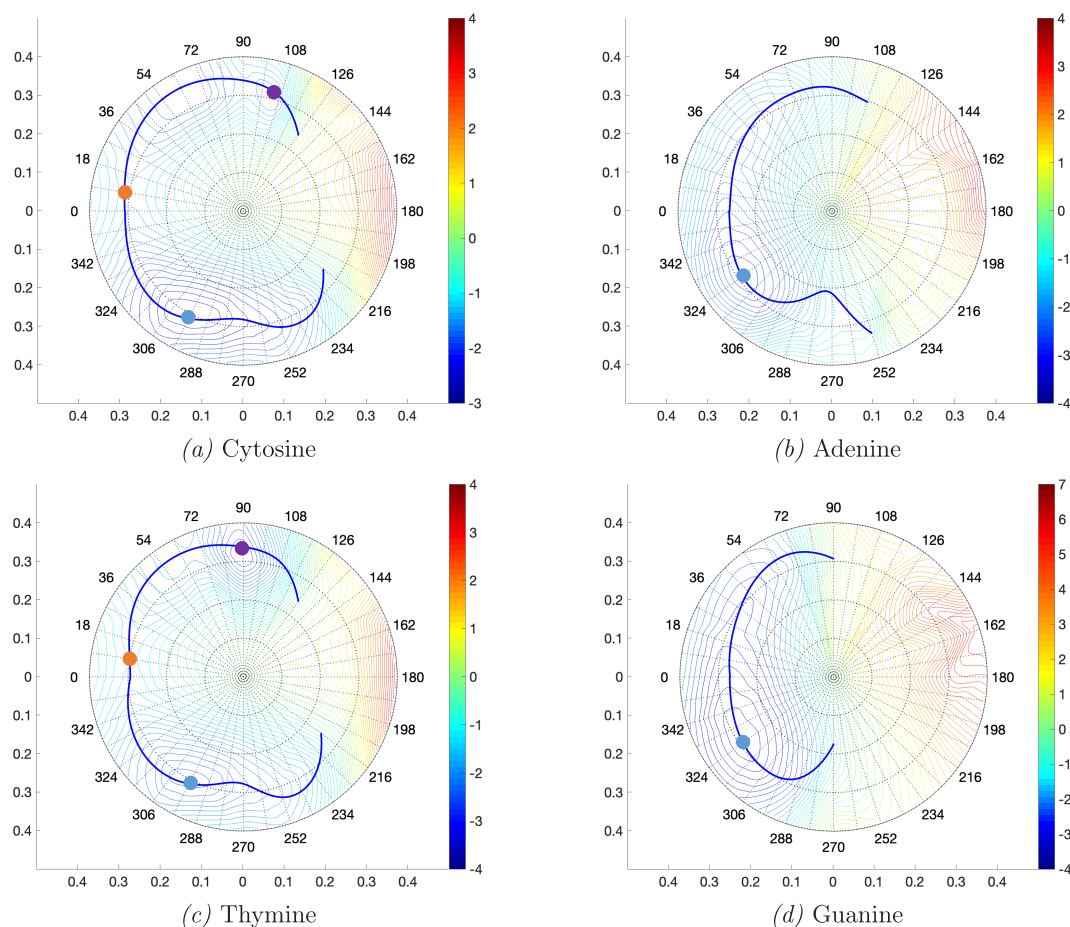
**Figure 13.** H-bond free deoxyribonucleoside analogs **dCm**, **dAm**, **dTm**, and **dGm**.

**dGm** only one minimum is found at  $\phi_2 = 342^\circ$  and the pseudolibration paths do not become considerably longer. This suggests that H-bonding invokes more strain on the pyrimidic bases, which is line with the above finding that pyrimidic H-bonding is more covalent in nature.

## CONCLUSIONS AND OUTLOOK

In this study, the Cremer–Pople ring puckering analysis and the Konkoli–Cremer local mode analysis supported by the topological analysis of the electron density were applied to systematically analyze for the first time the interplay between deoxyribose ring puckering and the intramolecular H-bonding in 2'-deoxycytidine (cytosine), **dC**, 2'-deoxyadenosine (adenine), **dA**, thymidine (thymine), **dT**, and 2'-deoxyguanosine (guanine), **dG**. Using Cremer–Pople puckering coordinates, the CES for any substituted ring system such as a deoxyribonucleoside can be determined in analytical form and a physically meaningful pseudorotation path is obtained. Local mode force constants are a unique measure of bond strength. Our work has led to the following conclusions:

1. We found for all four deoxyribonucleosides **dC**, **dA**, **dT**, and **dG** incomplete pseudorotation paths on the CESs



**Figure 14.** CESs and pseudolibration paths of the H-bond free deoxyribonucleosides **dCm** (a); **dAm** (b); **dTm** (c); and **dGm** (d). At the center of each CES, the planar deoxyribose ring form is located. The corresponding energy is used as reference. Both  $x$  and  $y$  axes show the magnitude of puckering amplitude  $q_2$  in angstroms. The outer radius of the CES represents the maximum puckering amplitude of 0.4 Å. The labels around CES circle denote the value of the phase angle  $\phi_2$  in degrees. The solid blue line indicates the pseudolibration path. The color bar represents the energy on the CES in kilocalories per mole relative to the planar form: (yellow to red regions) location of conformers higher in energy than the planar form; (green to blue regions) location of conformers lower in energy than the planar form. The purple dot in the range  $90^\circ$ – $108^\circ$  shows the location of the local, the blue dot near  $306^\circ$  the location of the global minimum, and the yellow dot near  $9^\circ$  the transition state between the two minima for **dCm** and **dTm**. The blue dot at  $324^\circ$  shows the single minimum for **dAm** and **dGm**. Calculated at the  $\omega$ B97X-D/6-31++G(d,p) level of theory.

caused by ring inversion, i.e. the pseudorotation path is not a closed circle but an open curve, which we coined as a pseudolibration path. On each of the pseudolibration paths a global minimum in the range of  $\phi_2 = 72^\circ$ – $90^\circ$  and a local minimum in the range of  $\phi_2 = 306^\circ$  separated by a transition state in the range of  $\phi_2 = 18^\circ$ – $342^\circ$  could be identified. Harmonic frequency calculations identified all conformers in the global and local minimum regions as minimum structures (no imaginary frequency) and that in the transition region as a transition structure (one imaginary frequency). In this regard, the pseudorotation path can be considered as a special reaction path with the phase angle  $\phi_2$  as a reaction coordinate. Studies of H-bond free deoxyribonucleoside analogs revealed that removal of the H-bond does not restore the full conformational flexibility of the sugar ring. For all analogs there exists still a pseudolibration path, which for the pyrimidic bases is considerably longer compared with their original counterparts. This reflects that H-bonding invokes more strain on the pyrimidic bases than on the puric bases.

- There are two major factors determining the conformational flexibility of the deoxyribonucleosides, ring puckering and internal H-bonding. Our work showed that ring puckering plays the dominant role. All deoxyribonucleosides feature the same deoxyribose ring puckering pattern, and strongest puckering occurs in the global minimum region ( $\phi_2 = 72^\circ$ – $90^\circ$ ,  $q_2$  values up to 0.35 Å), followed by the puckering in the local minimum region ( $\phi_2 = 288^\circ$ – $306^\circ$ ,  $q_2$  values up to 0.31 Å), while smallest puckering ( $q_2 = 0.15$ – $0.18$  Å) occurs in the transition region in the range of  $\phi_2 = 324^\circ$ – $54^\circ$ . This suggests that the larger the puckering amplitude, the lower the conformational energy. In contrast no direct correlation between conformational energy and H-bond strength could be found.
- We quantitatively assessed the H-bond strength of all conformers along the pseudorotation paths via bond strength orders BSO  $n$  derived from local vibrational force constants. We found a direct correlation between H-bond strength and H-bond length. Longest and weakest H-bonds were found in the local minimum region for all deoxyribonucleosides, whereas shortest and strongest H-

- bonds were found outside both the global minimum region at the turning points of the pseudolibration paths, where the deoxyribonucleosides bounce back into the opposite path direction. These results clearly reveal that H-bonding determines the shape and length of the pseudolibration paths. In addition to the H-bond strength we evaluated the covalent/electrostatic character of the H-bonds applying the Cremer–Kraka criterion of covalent bonding. H-bonding in the puric bases has more covalent character whereas for the pyrimidic bases the character of the H-bond is more electrostatic.
4. The formation of the internal H-bond is affected by the mutual orientation of the CH<sub>2</sub>OH group and the base which in turn depends on the puckering mode. The influence of this orientation on the H-bond formation was quantified via (i) two dihedral angles describing the rotation of the CH<sub>2</sub>OH group and the base perpendicular to the sugar ring and (ii) two angles describing the tilting of the CH<sub>2</sub>OH group and the base relative to the center of the deoxyribose ring. We found that the tilting movement is more pronounced for the puric bases although they are more bulky than their pyrimidic counterparts. Overall, our analysis suggests that side group rotation is more important for H-bond formation. Besides geometric factors the strength of the H-bond also depends on the orientation and electron density distribution of the lone pair of the H-bond acceptor atom (N, respectively O). We assessed both via the delocalization energy  $\Delta E_{\text{del}}(\text{HB})$ . With larger  $\Delta E_{\text{del}}(\text{HB})$  values corresponding stronger H-bonds were found along the pseudolibration paths for puric bases in line with our finding that H-bonding in the puric bases is of more covalent nature and that the global minimum conformation of dG has the strongest H-bond of all conformers investigated in this work with a BSO  $n$  value of 0.436, which is even stronger than the H-bond in the water dimer (BSO  $n = 0.360$ ).

Currently, we are applying our new analysis to the DNA building blocks deoxyribonucleotides, which possess a more complex internal H-bonding pattern caused by the phosphate group, and to the characterization of unnatural base pairs which have recently drawn a lot of attention.<sup>103,104</sup>

## ■ ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpca.9b05452.

Cut through the CES of Adenine for a fixed value of the puckering phase angle  $\phi_2$ . 3D plot of the CES for adenine. Geometries of dA, dG, dC, and dT at the global minimum, transition state, and local minimum (PDF)

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### Notes

The authors declare no competing financial interest.

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